Mathematical Ideas Chapter 2 Review

Name_____

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the cardinal number of the set.

1) The numbers in the Venn Diagram below represent cardinalities. 1) E 11 10 14 U c 7 Find n(B \cup C) A) 14 B) 60 C) 49 D) 42 2) $\{x \mid x \text{ is an even integer number smaller than 100}\}$ 2) D) א ₀ B) 99 A) c C) 49 3) 3) The numbers in the Venn Diagram below represent cardinalities. 11 10 14 U C 7 Find n(A \cap B' \cap C) A) 7 B) 15 C) 11 D) 6 4) {-4, -8, -12, -16,} 4) A) × 0 B) 4 C) c D) 100

1

| 5) Given: | | | | 5) |
|--|-------------------------------|---------------|---------------|-----|
| n(A) = 60 n(B) = 68 n(C) = 62 $n(A \cap B) = 12$ $n(A \cap C) = 14$ $n(B \cap C) = 8$ $n(A \cap B \cap C) = 6$ $n(A' \cap B' \cap C') = 121$ Find n(U) | | | | |
| | | | | |
| A) 293 | B) 222 | C) 283 | D) 162 | |
| 6) {The set of points on a strai | ght line} | | | 6) |
| А) × ₀ | B) 0 | C) 1 | D) c | |
| 7) {Monday, Tuesday,, Satu | ırday} | | | 7) |
| A) 7 | B) 3 | C) 4 | D) 6 | |
| Determine whether the sets are equa | al, equivalent, both, or nei | ther. | | |
| 8) {x x is an even integer } ar | nd {x x is an odd integer } | | | 8) |
| A) Both | B) Neither | C) Equivalent | D) Equal | |
| 9) {4, 13} and {4, 1, 3} | | | | 9) |
| A) Both | B) Equal | C) Equivalent | D) Neither | |
| 10) {brake} and {break} | | | | 10) |
| A) Neither | B) Both | C) Equal | D) Equivalent | |
| 11) {34, 45, 63} and {45, 63, 34} | | | | 11) |
| A) Both | B) Equal | C) Equivalent | D) Neither | |
| 12) {3, 14} and {31, 4} | | | | 12) |
| A) Neither | B) Both | C) Equal | D) Equivalent | |
| Find the indicated cardinal number. | | | | |
| 13) Find n(A) given that $n(A \times A)$ | B) = 108 and n(B) = 9. | | | 13) |
| A) 12 | B) 117 | C) 9 | D) 99 | |

| 14) Find n(F), given that n(B × F) = 18 and B = $\{1, 3\}$. | | | | |
|--|-----------------------------|------------------|-------|-----|
| A) 54 | B) 6 | C) 9 | D) 36 | |
| 15) Find n(E), given th | nat n(C × E) = 18 and C = { | 4, 5, 6}. | | 15) |
| A) 54 | B) 9 | C) 6 | D) 3 | |
| 16) Find n(C × D) give | en that C = {4, 5, 6} and D | = {7, 8, 9, 10}. | | 16) |
| A) 12 | B) 7 | C) 27 | D) 81 | |

The lists below show five agricultural crops in Alabama, Arkansas, and Louisiana.

| <u>Alabama</u> | <u>Arkansas</u> | <u>Louisiana</u> |
|----------------|-----------------|------------------|
| soybeans (s) | soybeans (s) | soybeans (s) |
| peanuts (p) | rice (r) | sugarcane (n) |
| corn (c) | cotton (t) | rice (r) |
| hay (h) | hay (h) | corn (c) |
| wheat (w) | wheat (w) | cotton (t) |

Let U be the smallest possible universal set that includes all of the crops listed, and let A, K and L be the sets of five crops in Alabama, Arkansas, and Louisiana, respectively. Find each of the following sets.

| 17) L' ∩ A | | | | 17) |
|-----------------------------|-------------------------------|--------------------------|--------------|-----|
| A) {c, s} | B) {h, n, t, w} | C) {n, r, t} | D) {h, p, w} | |
| 18) The set of crops in I | U. | | | 18) |
| A) {s, p, c, h, w, s | s, r, t, h, w, s, n, r, c, t} | B) {c, h, n, p, r, s, t, | , w} | |
| C) {s, p, c, h, w, r | r, t, n, c} | D) {s, p, c, w, r, t, n |)} | |
| 19) The set of crops cor | nmon to A, K, and L | | | 19) |
| A) {n, p, s} | | B) {c, h, n, p, r, s, t, | , w} | |
| C) {s} | | D) {n, p} | | |
| 20) The set of crops in A | ۹'. | | | 20) |
| A) {c, h, n, r, s, t, | w} | B) {r, t} | | |
| C) {h, n, r, t} | | D) {n, r, t} | | |
| 21) A ∩ K | | | | 21) |
| A) {h, s, w} | | B) {c, p, r, t} | | |
| C) {c, h, p, r, s, t, | w} | D) {c, h, s, t, w} | | |
| | | | | |

Decide whether or not it is possible to set up a one-to-one correspondence between the elements of the sets.

22) {0, 5, 12, 17} and {5, 12, 17} A) Not possible B) Possible 22)

23) {0} and {187}

A) Possible

24) {0, 0.5, 0.25, 0.2} and
$$\left\{\frac{1}{2}, \frac{1}{4}, \frac{1}{5}\right\}$$

A) Not possible

Shade the regions representing the set.



B) Not possible

B) Possible

A one-to-one correspondence between the set of counting numbers and the given set has been established. Find an expression for the nth term of the given set that corresponds to the counting number n.

28) 28) _____ **{-11**, **-22**, **-33**, **-44**, ..., □, ...**} \$ \$ \$ \$** \$ 1 2, 3, 4, ..., n, ...} {1, C) n + 11 A) -11n B) 11n D) n - 11

23)

24) _____

| 29) | | | | 29) |
|---|---------|----------|---------------------|-----|
| {100, 200, 300, 400, | , □,} | | | |
| $\mathbf{\hat{x}} \mathbf{\hat{x}} \hat{$ | \$ | | | |
| {1, 2, 3, 4, | , n,} | | | |
| A) 100 ⁿ | B) 100n | C) -100n | D) n ¹⁰⁰ | |
| | | | | |
| 30) | | | | 30) |
| {2, 5, 8, 11,, □,} | | | | |
| $\uparrow \uparrow $ | | | | |
| {1, 2, 3, 4,, n,} | | | | |
| Λ) 3n - 1 | | | | |

Show that the set has cardinal number \aleph_0 by establishing a one-to-one correspondence between the set of counting numbers and the given set. Be sure to show the pairing of the general terms in the sets.

| 31) {4, 8, 12, 16,} | | 31) |
|---|---|-----|
| A) { 1, 2, 3, 4,, n,} ↓ ↓ ↓ ↓ ↓ { 4, 8, 12, 16,, 4n,} | B) { 1, 2, 3, 4,, n,} ↓ ↓ ↓ ↓ ↓ { 4, 8, 12, 16,, n,} | |
| C) { 0, 1, 2, 3,, n,} $\downarrow \downarrow \downarrow \downarrow \downarrow$ { 4, 8, 12, 16,, 4n,} | D) { 1, 2, 3, 4,, n,} ↓ ↓ ↓ ↓ ↓ { 4, 8, 12, 16,, 5n,} | |
| 32) {3, 9, 27, 81,} | | 32) |
| A) { 1, 2, 3, 4,, n,} $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$ { 3, 9, 27, 81,, n ³ ,} C) { 1, 2, 3, 4,, n,} $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$ { 3, 9, 27, 81,, 3n,} Solve the problem. 33) A survey of 240 families showed that 91 had a dog; 70 had a cat; 31 had a dog and a cat; 91 had poither a cat par a dog par a parakeet; | B) { 1, 2, 3, 4,, n,} $\downarrow \downarrow \downarrow \downarrow \downarrow$ { 3, 9, 27, 81,, 3n,} D) { 1, 2, 3, 4,, n,} $\downarrow \downarrow \downarrow \downarrow \downarrow$ { 3, 9, 27, 81,, 32n,} | 33) |
| 7 had a cat, a dog, and a parakeet. | | |
| How many had a parakeet only? | | |
| A) 29 B) 34 | C) 24 D) 19 | |
| 34) Mrs. Bollo's second grade class of thirty students co survey indicate that 8 students own a cat, 15 studen a dog. How many of the students surveyed own on | nducted a pet ownership survey. Results of the its own a dog, and 5 students own both a cat and ly a cat? | 34) |

A) 8 B) 18 C) 3 D) 15

| 35) Monticello residen an upcoming elect both Moore and A | 35) Monticello residents were surveyed concerning their preferences for candidates Moore and Allen in an upcoming election. Of the 800 respondents, 300 support neither Moore nor Allen, 100 support both Moore and Allen, and 250 support only Moore. How many residents support Moore or Allen? | | | 35) |
|---|---|---|---|-----|
| A) 300 | B) 100 | C) 400 | D) 500 | |
| 36) A survey of 118 co = the set of those ta taking canoeing. T $n(A) = 45$ $n(A \cap$ $n(B) = 55$ $n(A \cap$ $n(C) = 40$ $n(B \cap$ $n(A \cap B \cap C) = 2$ | llege students was done to aking art, B = the set of tho he study revealed the follo B) = 12 C) = 15 C) = 23 | find out what elective co se taking basketweaving, wing information. | urses they were taking. Let A and C = the set of those | 36) |
| How many studen | ts were not taking any of t | hese electives? | | |
| A) 10 | B) 28 | C) 36 | D) 26 | |
| 37) A survey of a grou 66 of the tourists p 50 plan to visit the 10 plan to visit the 14 plan to visit the 18 plan to visit the 9 plan to visit the 14 plan to visit nor | p of 116 tourists was taker lan to visit Gateway Arch; zoo; Art Museum and the zoo, Art Museum and the Gate Gateway Arch and the zoo Art Museum, the zoo, and he of the three places. | n in St. Louis. The survey but not the gateway Arch eway Arch, but not the zo o, but not the Art Museur I the Gateway Arch; | showed the following: n; o; n; | 37) |
| How many plan to | visit the Art Museum onl | y? | | |
| A) 13 | B) 50 | C) 37 | D) 102 | |
| Use \subseteq or $\not\subseteq$ in the blank to m | ake a true statement. | | | |
| 38) {6, 8, 10} {5, 6, 7 | 8, 10} | | | 38) |
| A) ⊈ | | B) ⊆ | | |
| 39) {b, p, a} {b, b, p, | p, a, a} | | | 39) |
| A) ⊈ | - · · | B) ⊆ | | - |

Draw an appropriate Venn diagram and use the given information to fill in the number of elements in each region.

40)

41)



41) n(A) = 35, $n(A \cap B') = 24$, $n(A \cap C) = 15$, $n(B \cap C) = 14$, $n(A' \cap B' \cap C') = 10$, $n(A \cap B \cap C) = 6$, $n(B \cup C) = 52$, $n(B \cap C') = 18$



Complete the blank with either \in or \notin to make the statement true.

| 42) {3} _ {4 - 3, 5 - 3, 6 - 3, 7 - | - 3} | | | 42) |
|-------------------------------------|--------------------------|----------------|----------------|-----|
| A) ∈ | | B) ∉ | | |
| 43) a {A, B, C,, Z} | | | | 43) |
| A) ∉ | | B) ∈ | | · |
| Describe the conditions under whic | h the statement is true. | | | |
| 44) A ∪ B = A | | | | 44) |
| A) B = Ø | B) B ⊆ A | C) A ⊆ B | D) Always true | |
| 45) A ∩ A' = A | | | | 45) |
| A) A = U | B) A ≠ Ø | C) Always true | D) A = Ø | |

| | 46) A ∩ B' = A | | | | 46) |
|---------------------------------|---|----------------------------|-----------------------------|------------------------|----------------|
| | A) A ∩ B = ∅ | B) Always true | C) B = ∅ | D) B ⊆ A | |
| | 47) A ∩ B = A | | | | 47) |
| | A) B ⊆ A | B) A ⊆ B | C) Always true | D) B = Ø | |
| Let A false. | and B be sets with cardina | I numbers, n(A) = a and n | (B) = b, respectively. Deci | de whether the stateme | ent is true or |
| | 48) If $B \subseteq A$, $n(B) = n(A)$ - | n(A - B). | | | 48) |
| | A) True | | B) False | | |
| | 49) n(A ∪ B) = n(A) - n(B) | | | | 49) |
| | A) True | | B) False | | |
| List tl | ne elements in the set. | | | | |
| | 50) The set of all positive i | nteger powers of 3. | | | 50) |
| | A) {1, 8, 27, 64, 125, | } | B) {3, 9, 27, 81, 243, | .} | |
| | C) {1, 3, 9, 27, 81, 24 | 3,} | D) {3, 6, 9, 12, 15,} | | |
| | 51) { x x is an even integ | er smaller than 8} | | | 51) |
| | A) {, -6, -4, -2, 0, 2 | 2, 4, 6} | B) {, -6, -4, -2, 2, 4, | 6} | |
| | C) {2, 4, 6} | | D) {0, 2, 4, 6} | | |
| | 52) {x x is an integer betw | veen 3 and 7} | | | 52) |
| | A) {4, 5, 6, 7} | B) {3, 4, 5, 6} | C) {4, 5, 6} | D) {3, 4, 5, 6, 7} | |
| | 53) The set of all whole nu | mbers greater than 3 and I | ess than 7 | | 53) |
| | A) {3, 4, 5, 6} | B) {4, 5, 6} | C) {4, 5, 6, 7} | D) {3, 4, 5, 6, 7} | |
| List tl Let U A B C | ne elements in the set . = {q, r, s, t, u, v, w, x, y, z} = {q, s, u, w, y} = {q, s, y, z} = {v, w, x, y, z}. | | | | |
| | 54) C' ∪ A' | | | | 54) |
| | A) {s, t} | | B) {q, r, s, t, u, v, x, z] | ł | |
| | C) {w, y} | | D) {q, s, u, v, w, x, y, | Z} | |
| | 55) A ∩ B' | | | | 55) |
| | A) {t, v, x} | | B) {r, s, t, u, v, w, x, z | :} | |
| | C) {q, s, t, u, v, w, x, | y} | D) {u, w} | | |

| Write the set in set-builder nota | tion. | | | |
|--|----------------------------|---------------------------------|----------------------|-----|
| 56) The set of all cars own | ed by students | | | 56) |
| A) {x is a student wi | th a car} | B) {x is a car} | | |
| C) {x x is a student | t with a car} | D) {x x is a car owr | ned by a student} | |
| 57) {17, 18, 19, 20} | | | | 57) |
| A) {17, 18, 19, 20} | | B) {x x is an intege | r less than 21} | |
| C) {x x is an intege | er between 16 and 21} | D) {x x is an intege | r between 17 and 20} | |
| 58) {, -3, -2, -1, 0, 1, 2, 3, | } | | | 58) |
| A) {x x is any integ | jer greater than -3} | B) {x x is a natural | number} | |
| C) {x x is an intege | r} | D) {-3, -2, -1, 0, 1, 2, | 3} | |
| Find the number of proper subs | sets of the set. | | | |
| 59) {3, 4, 5} | | | | 59) |
| A) 7 | B) 2 | C) 5 | D) 6 | |
| 60) {x x is an even numb | er between 15 and 29} | | | 60) |
| A) 128 | B) 64 | C) 28 | D) 127 | |
| Write a description of the shade | d region using the symbol | Is A, B, C, ∪, ∩, -, and ′ as i | needed. | 61) |
| | | | | ., |
| A) C ∩ B′ ∪ A | B) B′ ∩ A ∪ C | C) A ∪ C | D) A ∪ C - B | |
| 62) | | | | 62) |
| Â B C | | | | |
| A) (A' ∪ B) ∩ C | B) A' ∩ C | C) (A' ∩ B) ∪ C | D) (A ∪ B') ∩ C | |
| Decide whether \subseteq , \subset , both, or ne | ither can be placed in the | blank to make a true state | ement. | |

| 63) {s, r, t} {s, r, t} | | | | 63) |
|-----------------------------------|------------|------|------|-----|
| A) Both \subseteq and \subset | B) Neither | C) ⊆ | D) ⊂ | |

| 64) Ø{3, 17, 30, 42} | | | | 64) |
|-----------------------------------|------------------|-----------------------|-------------|-----|
| A) Both \subset and \subseteq | B) ⊆ | C) Neither | D) ⊂ | |
| Decide whether the given statemen | t is always true | e or not always true. | | |
| 65) (A ∩ B) ⊆ B | | | | 65) |
| A) Not always true | | B) Always true | | |
| 66) A - A' = A | | | | 66) |
| A) Always true | | B) Not always true | | |
| 67) (A ∪ B) ⊆ A | | | | 67) |
| A) Always true | | B) Not always true | | |

Show that the set is infinite by placing it in a one-to-one correspondence with a proper subset of itself. Be sure to show the pairing of the general terms in the sets.

| $68) \left\{ \frac{4}{9}, \frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \dots \right\}$ | | 68) |
|---|---|-----|
| A) $\left\{ \frac{4}{9}, \frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \dots, \frac{n}{9}, \dots \right\}$ | B) $\left\{ \frac{4}{9}, \frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \dots, \frac{n+4}{9}, \dots \right\}$ | |
| $\downarrow \downarrow \downarrow \downarrow$ | \checkmark \downarrow \downarrow \downarrow \downarrow | |
| $\left\{\frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \frac{8}{9}, \dots, \frac{n+1}{9}, \dots\right\}$ | $\left\{\frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \frac{8}{9}, \dots, \frac{n+5}{9}, \dots\right\}$ | |
| C) $\left\{ \frac{4}{9}, \frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \dots, \frac{n-4}{9}, \dots \right\}$ | D) $\left\{ \frac{4}{9}, \frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \dots, \frac{n+3}{9}, \dots \right\}$ | |
| $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$ | $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$ | |
| $\left\{\frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \frac{8}{9}, \dots, \frac{n-5}{9}, \dots\right\}$ | $\left\{\frac{5}{9}, \frac{6}{9}, \frac{7}{9}, \frac{8}{9}, \dots, \frac{n+4}{9}, \dots\right\}$ | |

Find n(A) for the set.

| 69) A = {2, 4, 6, 8, 10} | | | | 69) |
|--------------------------|--------------|-------------|-------------|-----|
| A) n(A) = 4 | B) n(A) = 10 | C) n(A) = 2 | D) n(A) = 5 | |

| 70) A = {x x is a month in the year} | | | | 70) |
|--|-------------|--------------|--------------|-----|
| A) n(A) = 12 | B) n(A) = 1 | C) n(A) = 24 | D) n(A) = 52 | |

Let U = {all soda pops}, A = {all diet soda pops}, B = {all cola soda pops}, C = {all soda pops in cans}, and D = {all caffeine-free soda pops}. Describe the set in words.

71) (A ∪ D) ∩ C' 71)

A) All diet, caffeine-free soda pops not in cans

B) All diet soda pops not in cans or all caffeine-free soda pops not in cans

C) All non-cola soda pops not in cans

D) All non-diet, non-caffeine-free soda pops not in cans

| Find the cardinal number of the indicated set. Use the cardinal number formula. 72) If $n(A) = 16$, $n(B) = 45$ and $n(A \cup B) = 53$, what is $n(A \cap B)$? | | | | 72) |
|--|---------------------------|------------------|------|-----|
| A) 8 | B) 10 | C) 24 | D) 4 | , |
| Determine whether the stat Let $A = \{1, 3, 5, 7\}$ $B = \{5, 6, 7, 8\}$ $C = \{5, 8\}$ $D = \{2, 5, 8\}$ $U = \{1, 2, 3, 4, 5, 6, 7, 8\}$ | ement is true or false. | | | |
| 73) Ø ⊆ A | | | | 73) |
| A) True | | B) False | | |
| Tell whether the statement | is true or false. | | | |
| 74) {x x is a counting number greater than 36} = {36, 37, 38,} | | | | 74) |
| A) True | | B) False | | |
| Determine whether or not t | he set is well defined. | | | |
| 75) {x x is a football | team that has won the Sup | er Bowl} | | 75) |
| A) Well defined | k | B) Not well defi | ned | |